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Sixth Semester B.E. Degree Examination, June/July 2011
Modeling & Finite Element Analysis

Time: 3 hrs.

Max. Marks:100

Note: Answer FIVE full questions selecting at least TWO questions from each part.

PART – A

- 1 a. Explain plane stress and plane strain cases with examples. (04 Marks)
- b. Find an expression for the displacement at the loading point for the bar shown in Fig. Q1 (b).

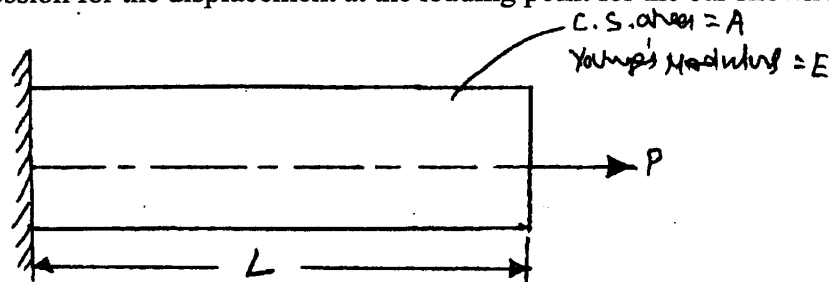


Fig. Q1 (b)

(10 Marks)

- c. Evaluate the following integral using two-point Gauss integration method:

$$I = \int_{-1}^{+1} (a_0 + a_1x + a_2x^2 + a_3x^3 + a_4x^4) dx.$$

(06 Marks)

- 2 a. Write the general description of the finite element method. (10 Marks)
- b. Write down the properties of stiffness matrix. (05 Marks)
- c. Explain node numbering scheme for a finite element mesh. (05 Marks)
- 3 a. Write down the general guidelines for selecting the interpolation polynomial. (03 Marks)
- b. Derive shape function for a 1-D bar element in terms of global coordinates. (07 Marks)
- c. Derive shape function for a 2-D simplex triangular element in terms of local coordinates. (10 Marks)
- 4 a. Derive interpolation polynomial (Shape functions) for 1-D quadratic element. (10 Marks)
- b. Derive shape functions for Isoparametric Linear Quadrilateral element in terms of local coordinates. (10 Marks)

PART – B

- 5 a. Explain different approaches used in developing element stiffness matrices and load vectors in FEM. (05 Marks)
- b. Derive stiffness matrix for a 1-D bar element under axial loading. (05 Marks)
- c. Derive strain-displacement matrix [B] for a isoparametric linear triangular element. (10 Marks)
- 6 a. Write down the differential equation governing the heat conduction in an orthotropic solid body and describe each term. (06 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and/or equations written eg. 42+8 = 50, will be treated as malpractice.

- b. Find the temperature distribution in the 1-D fin shown in Fig. Q6 (b). Take two elements for FE idealisation.

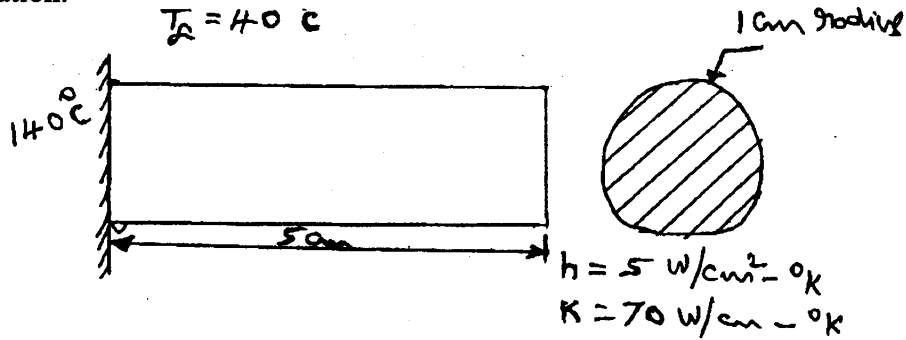


Fig. Q6 (b)

(14 Marks)

- 7 a. Describe different methods of applying boundary conditions in FEM. (06 Marks)
 b. For the two-bar truss shown in Fig. Q7 (b), determine the modal displacements through FEM. Take $E = 210 \times 10^9 \text{ Pa}$; $A = 0.01 \text{ m}^2$.

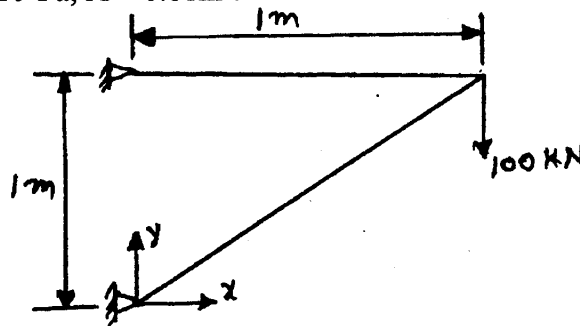


Fig. Q7 (b)

(14 Marks)

- 8 A uniform cross sectional beam is fixed at one end and supported by a roller at the other end. A concentrated load 20kN is applied at the mid length of the beam as shown in Fig. Q8. Determine the reflection under load.

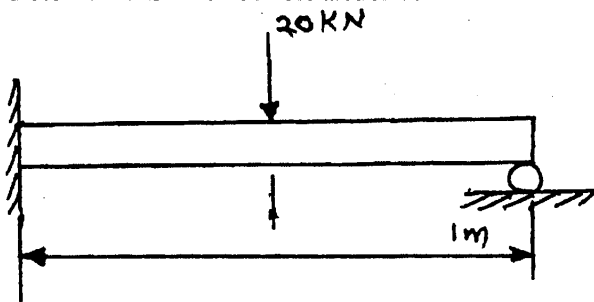


Fig. Q8

$E = 210\text{ GPa}$
 $I = 2500\text{ mm}^4$

(20 Marks)
